

Laws of Indices — Solved Practice Questions

This exercise set applies the laws of indices to fully worked examples — simplifying expressions, evaluating powers and roots, and expressing results in index form. **Perfect for students preparing for WAEC, NECO, and JAMB Mathematics.**

Exercises

1. If $2^n = y$, find $2^{2+n/3}$.
2. Simplify: $\sqrt{[(8^2 \times 4^{n+1}) \div (2^{2n} \times 16)]}$
3. Simplify $(a^2b^{-3}c)^{3/4} \div (a^{-1}b^4c^5)$ and express in the form $a^pb^qc^r$. Find $p + 2q$.
4. Simplify $16^{-1/2} \times 4^{-1/2} \times 27^{1/3}$
5. Evaluate $(4^{1/2} + 125^{1/3})^2$
6. Simplify $(6^{2/3} \times 8^{1/3}) \div 12^{2/3}$
7. Without using tables, evaluate $(0.027)^{-1/3} \times (0.09)^{3/2}$
8. Simplify $(3^{2a+1} \times 9^a \times 4^{2a}) \div (18^a \times 2^a \times 6^{2a})$

Note: Question 3 is printed here as $a^2b^{-3}c$ (with a negative power on b) — this is the reading that reproduces the answer -10 from the original video. The version with a^2b^3c (positive power on b) does not give -10, so it has been corrected here.

ANSWERS & WORKINGS

1. $2^{2+n/3} = 2^2 \times 2^{n/3} = 4 \times (2^n)^{1/3} = 4y^{1/3}$. **Answer: $4y^{1/3}$**
2. $8^2 = 2^6$; $4^{n+1} = 2^{2n+2}$; numerator = 2^{2n+8} . Denominator: $2^{2n} \times 16 = 2^{2n+4}$. Ratio = $2^4 = 16$. $\sqrt{16} = 4$. **Answer: 4**
3. $(a^2b^{-3}c)^{3/4} = a^{3/2}b^{-9/4}c^{3/4}$. Dividing by $a^{-1}b^4c^5$ gives $a^{3/2+1}b^{-9/4-4}c^{3/4-5} = a^{5/2}b^{-25/4}c^{-17/4}$. So $p = 5/2$, $q = -25/4$. $p + 2q = 5/2 - 25/2 = -10$. **Answer: -10**
4. $16^{-1/2} = 1/4$; $4^{-1/2} = 1/2$; $27^{1/3} = 3$. Product = $(1/4)(1/2)(3) = 3/8$. **Answer: 3/8**
5. $4^{1/2} = 2$; $125^{1/3} = 5$; sum = 7; $7^2 = 49$. **Answer: 49**
6. $8^{1/3} = 2$, so expression = $2 \times (6/12)^{2/3} = 2 \times (1/2)^{2/3} = 2^{1-2/3} = 2^{1/3} = \sqrt[3]{2}$. **Answer: $\sqrt[3]{2}$ (cube root of 2)**
7. $0.027 = (3/10)^3$, so $(0.027)^{-1/3} = 10/3$. $0.09 = (3/10)^2$, so $(0.09)^{3/2} = (3/10)^3 = 0.027$. Product = $(10/3) \times 0.027 = 0.09$. **Answer: 0.09**
8. $9^a = 3^{2a}$, $4^{2a} = 2^{4a}$, numerator = $3^{4a+1}2^{4a}$. $18^a = 2^a3^{2a}$, $6^{2a} = 2^{2a}3^{2a}$, denominator = $2^{4a}3^{4a}$. Ratio = $3^{4a+1-4a} = 3$. **Answer: 3**

✓ Questions 1, 2, 4, 5, 6, 7, and 8 have been checked and match the original answers exactly. Question 3 matches the original answer (-10) once read with a negative power on b , as explained above.

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